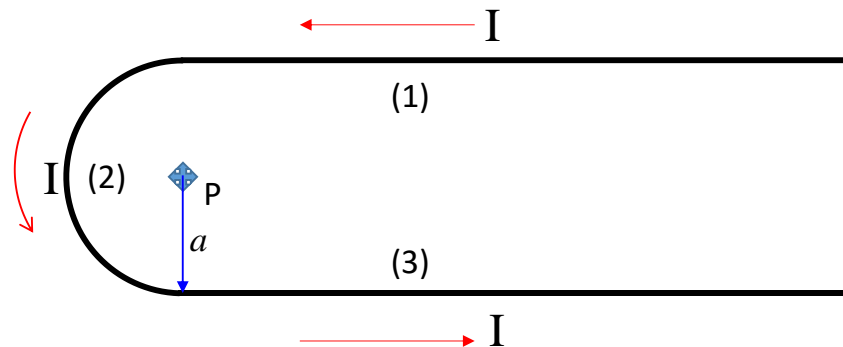




Sheet 11

- (1) Determine the magnetic flux density of a straight current filament of length L and current intensity I .
- (2) Determine the magnetic flux density at any point on the axis of a circular current loop of radius a flown by current I .
- (3) Determine the magnetic flux density at a point P of a straight pieces of current carrying wire shown in the figure of length L , and a current carrying semi-circle of radius $a = 5\text{cm}$ for $I = 2\text{A}$.



- (4) a) A filament is formed into a circle of radius a , centered at the origin in the plane $z = 0$. It carries a current I in the a_ϕ direction. Find H at the origin.
 b) A filament of the same length is shaped into a square in the $z = 0$ plane. The sides are parallel to the coordinate axes and a current I flows in the general a_ϕ direction. Again, find H at the origin.
- (5) Let a filamentary current of 5 mA be directed from infinity to the origin on the positive z axis and then back out to infinity on the positive x axis. Find: H at $M(0, 1, 0)$
- (6) a) Find H in Cartesian components at $P(2, 3, 4)$ if there is a current filament on the z axis carrying 8mA in the a_z direction.
 b) Repeat if the filament is located at $x = -1, y = 2$.
 c) Find H if both filaments are present
- (7) An infinite filament on the z axis carries $20\pi\text{ mA}$ in the a_z direction. Three a_z -directed uniform cylindrical current sheets are also present: 400 mA/m at $\rho = 1\text{ cm}$,



-250 mA/m at $\rho = 2$ cm and -300 mA/m at $\rho = 3$ cm. Calculate H at $\rho = 0.5, 1.5, 2.5,$ and 3.5 cm.

(8) The cylindrical shell, $2\text{mm} < \rho < 3\text{mm}$, carries a uniformly-distributed total current of 8A in the $-a_z$ direction, and a filament on the z axis carries 8A in the a_z direction. Find H everywhere

(9) A conducting filament at $\rho = 0$ carries 12 A in the a_z direction. Let $\mu_r = 1$ for $\rho < 1$ cm, $\mu_r = 6$ for $1 < \rho < 2$ cm, and $\mu_r = 1$ for $\rho > 2$ cm. Find

a) H everywhere

b) B everywhere

(10) Point P (2, 3, 1) lies on the planar boundary separating region 1 from region 2. The unit vector $a_{N12} = 0.6a_x + 0.48a_y + 0.64a_z$ is directed from region 1 to region 2. Let $\mu_{r1} = 2$, $\mu_{r2} = 8$ and $H_1 = 100a_x - 300a_y + 200a_z$ A/m. Find H_2

(11) Let $\mu_{r1} = 2$ in region 1, defined by $2x + 3y - 4z > 1$, while $\mu_{r2} = 5$ in region 2 where $2x + 3y - 4z < 1$. In region 1, $H_1 = 50a_x - 30a_y + 20a_z$ A/m.

Find:

a) H_{N1} (normal component of H_1 at the boundary)

b) H_{T1} (tangential component of H_1 at the boundary)

c) H_{T2} (tangential component of H_2 at the boundary)

d) H_{N2} (normal component of H_2 at the boundary)

e) θ_1 , the angle between H_1 and a_{N21}

f) θ_2 , the angle between H_2 and a_{N21}

(12) Three planar current sheets are located in free space as follows:

$-100a_x$ A/m at $z = -1$, $200a_x$ A/m at $z = 0$, $-100a_x$ A/m at $z = 1$.

Let $w_H = (1/2) \nabla \cdot H$ J/m³, then find w_H for all z.